

BIO 285/CSCI 285/MATH 285

Bioinformatics

Programming Lecture 9

Sequence Alignment 3

Dynamic Programming

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Alignment

Calculate scores of an alignment:

```
def score(s1, s2):  
    sc = 0  
    for i in range(len(s1)):  
        if s1[i]==s2[i]:  
            sc+= 20  
        elif (s1[i]=='A' and s2[i]=='G') or \  
            (s1[i]=='G' and s2[i]=='A'):  
            sc+=10  
        #.....  
    return sc
```

```
strand1 = "ACTCCG"  
strand2 = "CGACGC"  
print score(strand1, strand2)
```

Alignment

Calculate scores of an alignment – using dictionaries:

```
scoreTable={ "AA":20, "AC":5, "AG":10, "AT":5, |  
             "CA":5, "CG":5, "CC":20, "CT":5, |  
             "GA":10, "GC":5, "GG":20, "GT": 5, |  
             "TA":5, "TC":10, "TG":5, "TT": 20 }
```

```
def score(s1, s2):  
    sc = 0  
    for i in range(len(s1)):  
        pair = s1[i]+s2[i]  
        sc+=scoreTable[pair]  
    return sc
```

```
strand1 = "ACTCCG"  
strand2 = "CGACGC"  
print score(strand1, strand2)
```

Alignment

Another scoring method:

Match:	1
Mismatch:	-1
Gap:	-4
Extend Gap:	-1

```
ACTCT-CTGCCCTGCTGG
  CTATAC---CCTGCTGGG
  MMSMGMGEEMMMMMMMM
```

M: Match

S: Mismatch

G: Gap

E: Extend

11 Matches, 1 mismatch, 2 gaps, 2 extended gaps

Score = $11 - 1 - 2 * 4 - 2 = 1$.

Alignment

Alignment Games:

UIUC TechEnG Alignment Game:

1. Sequence Alignment Game

<http://teacheng.illinois.edu/SequenceAlignment/>

2. Dynamic Programming Game

<http://teacheng.illinois.edu/SequenceAlignmentDP/>

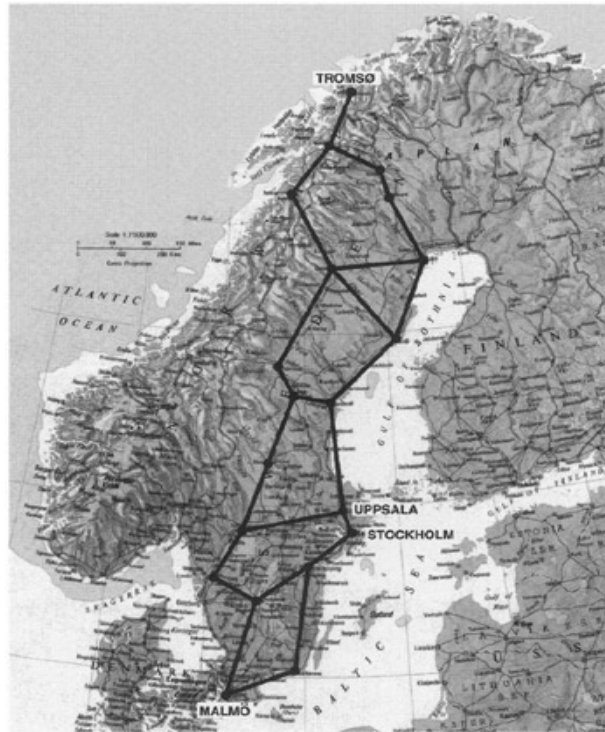
Phylo

<http://phylo.cs.mcgill.ca/>

Alignment

The dynamic programming: solving complex problems by breaking them down into simpler subproblems

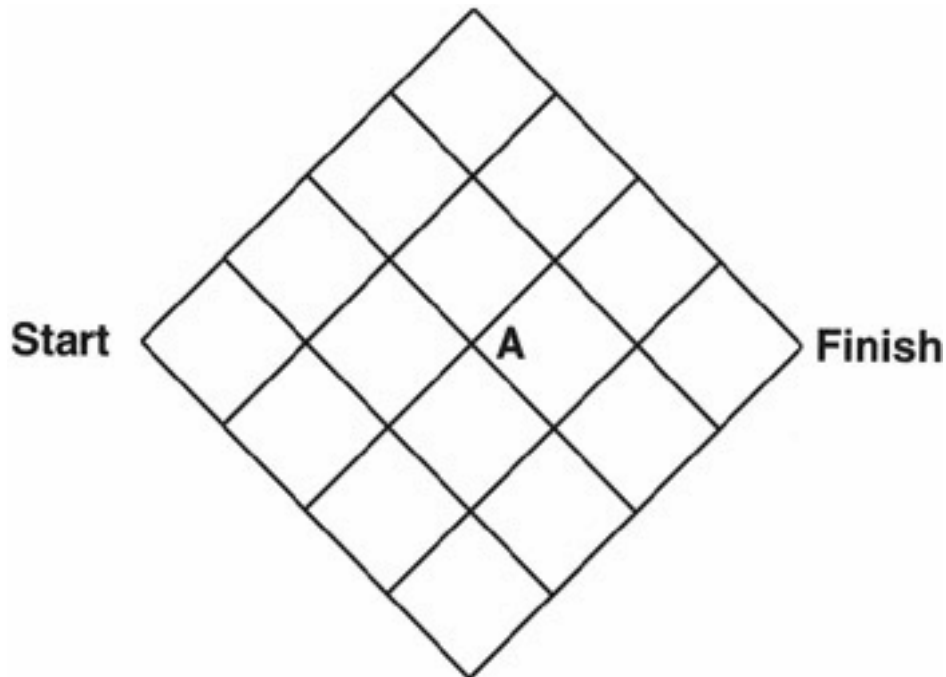
Example: Find the shortest path in a graph.



Alignment

The dynamic programming

The shortest path from Start to Finish through A must consist of the shortest path from Start to A and the shortest path from A to Finish.



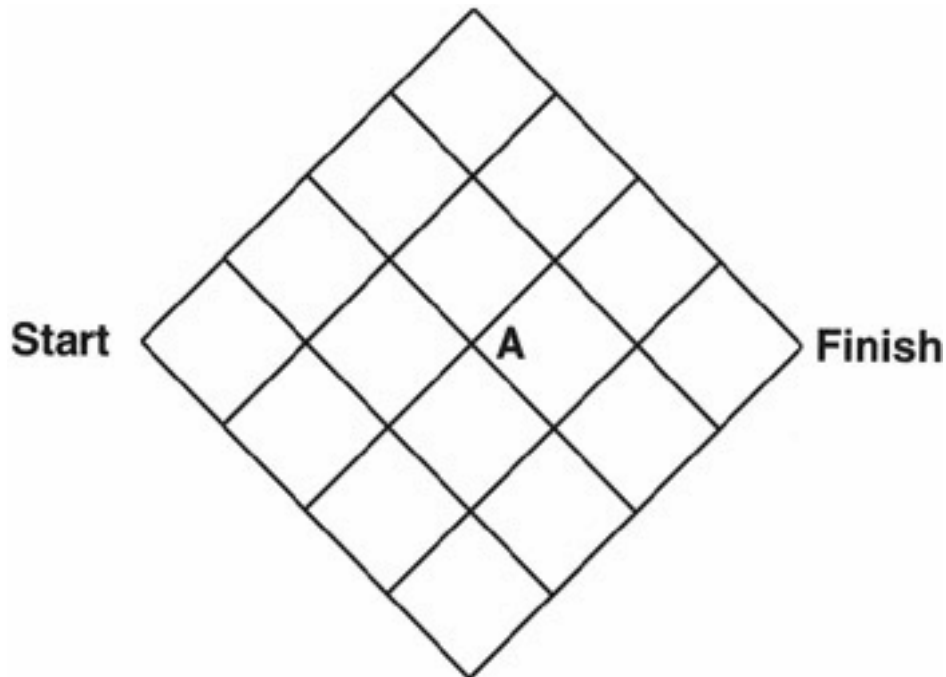
Alignment

Dynamic programming :

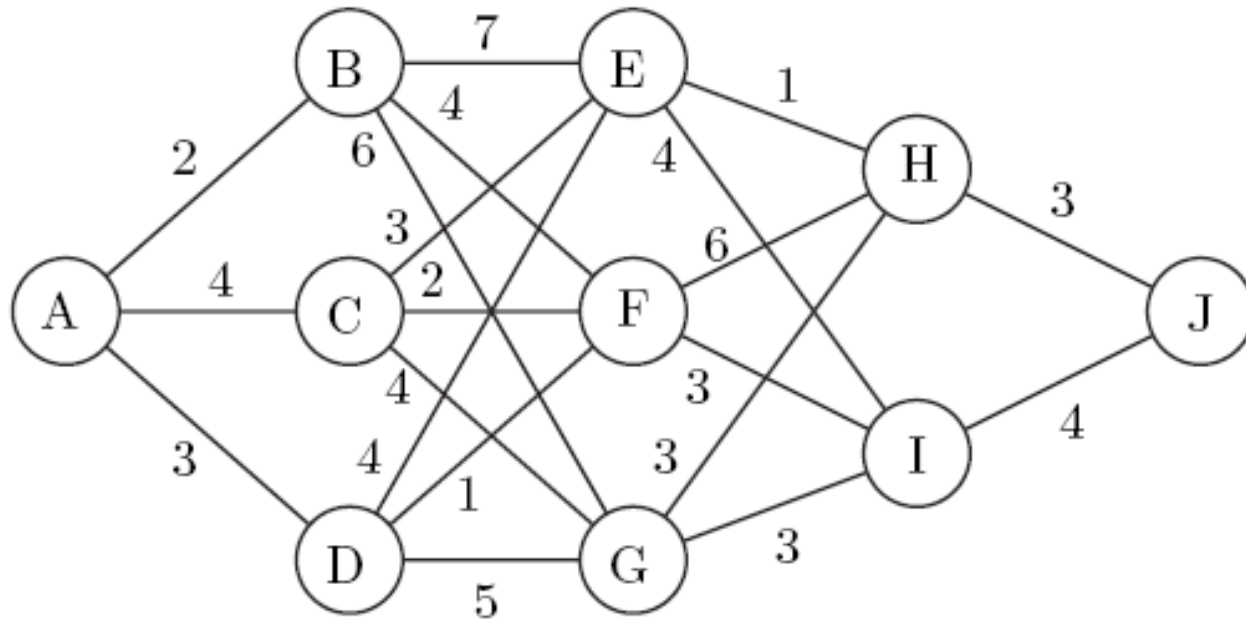
An abstract version of the problem:

There are 6 paths from start to A and 6 paths from A to finish.

There are 36 total possible path from start to finish through A.

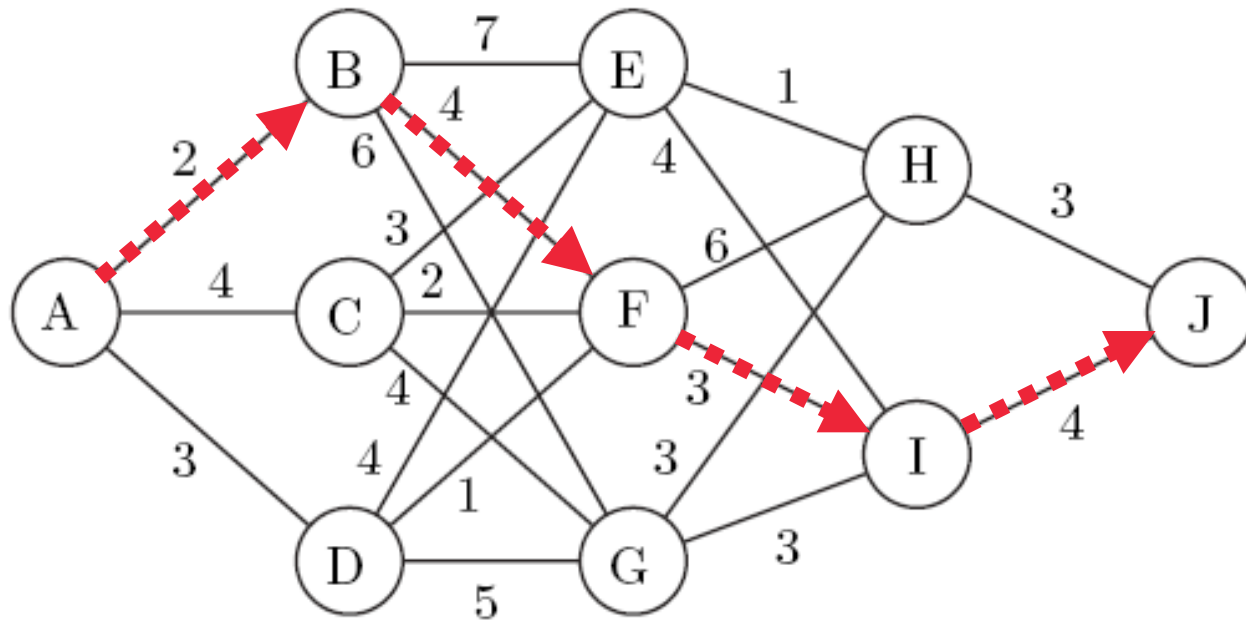


Stagecoach problem



A traveler wishes to minimize the length of a journey from town **A** to **J**.

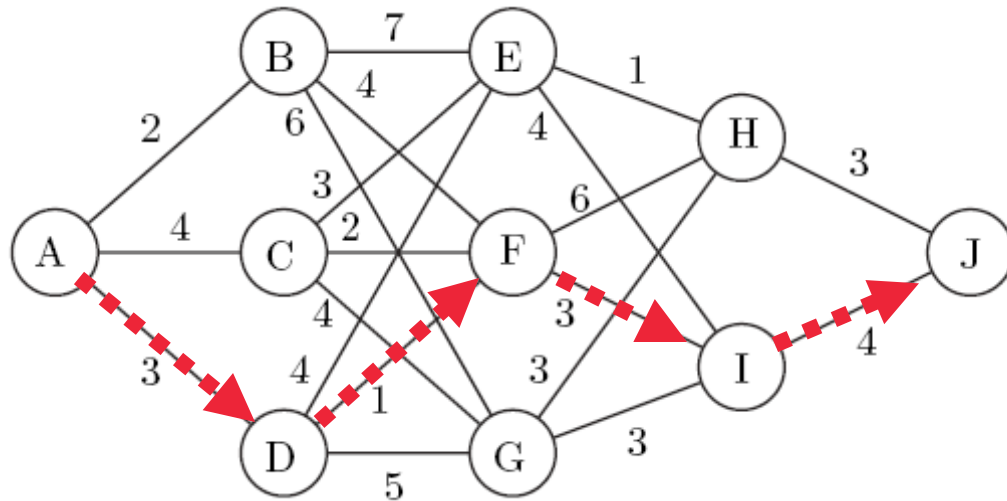
Greedy algorithm



The length of the route A-B-F-I-J: $2+4+3+4=13$.

Can we find shorter route?

Exhaustive search: try all

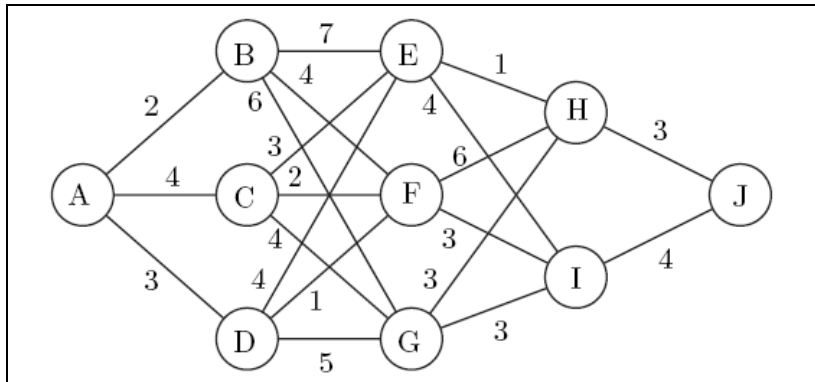
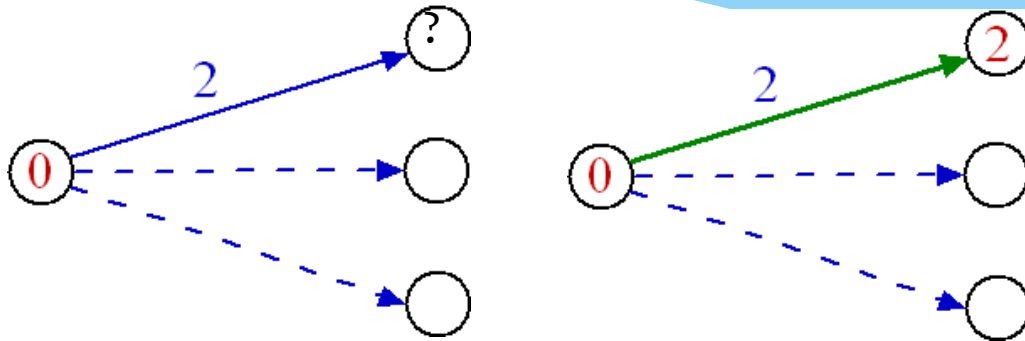


Route A-D-F-I-J: $3+1+3+4=11$

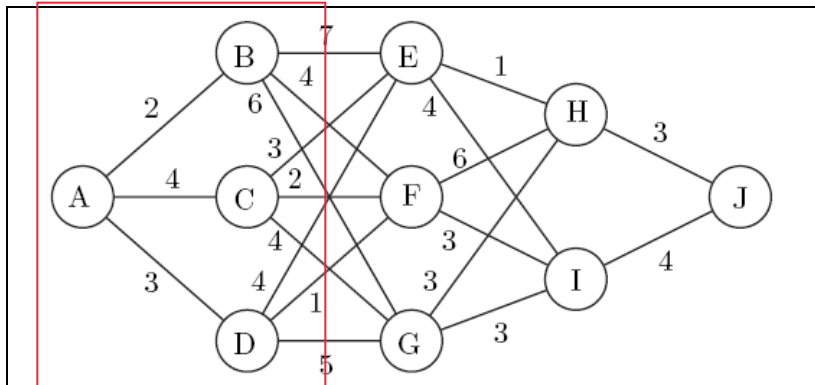
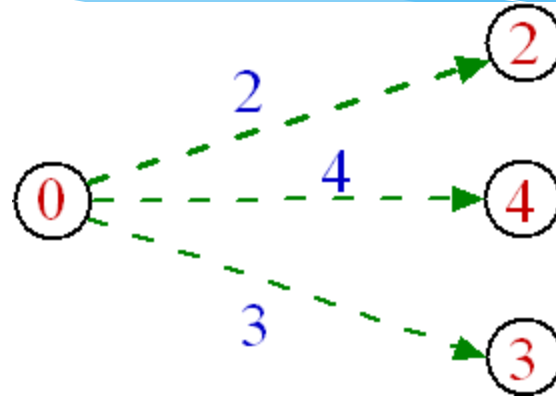
The total number of routes to be tested: $3 \times 3 \times 2 \times 1 = 18$

Can we avoid exhaustive search?

Shortest path construction: 1st stage (B)



Shortest path construction: 1st stage

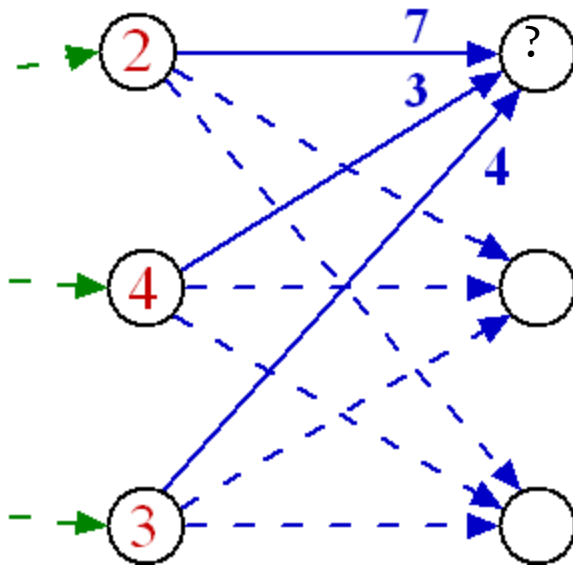


$$S(A,B)=2$$

$$S(A,C)=4$$

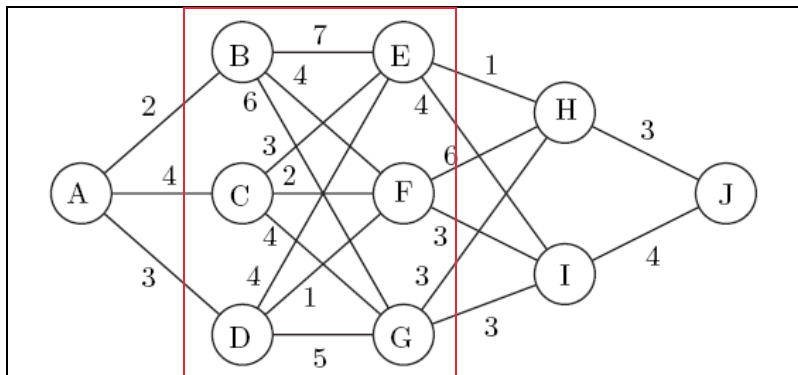
$$S(A,D)=3$$

Shortest path construction: 2nd stage (E)

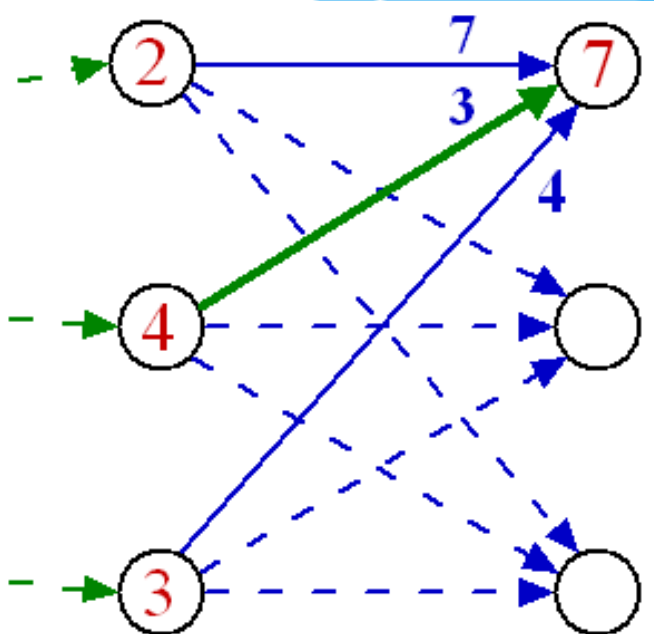


1. (A..B)-E: $2+7=9$
2. (A..C)-E: $4+3=7$
3. (A..D)-E: $3+4=7$

 (A..C)-E: 7

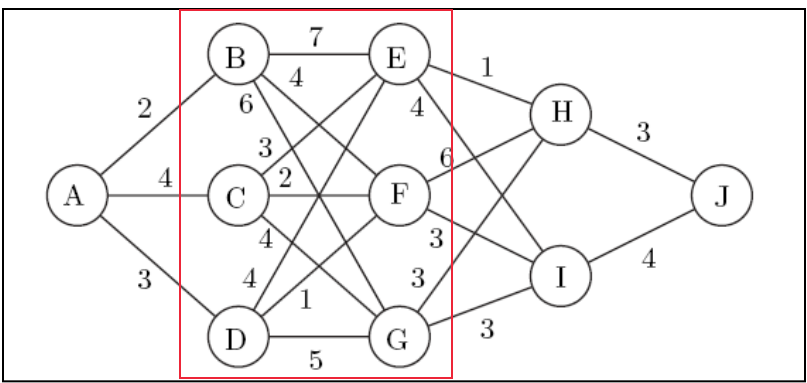


Shortest path construction: 2nd stage (E)

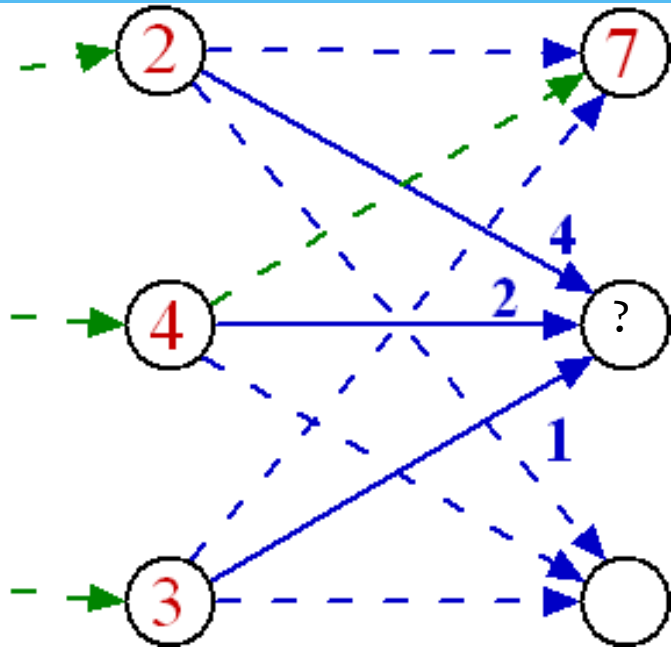


1. (A..B)-E: $2+7=9$
2. (A..C)-E: $4+3=7^*$
3. (A..D)-E: $3+4=7$

 (A..C)-E: 7

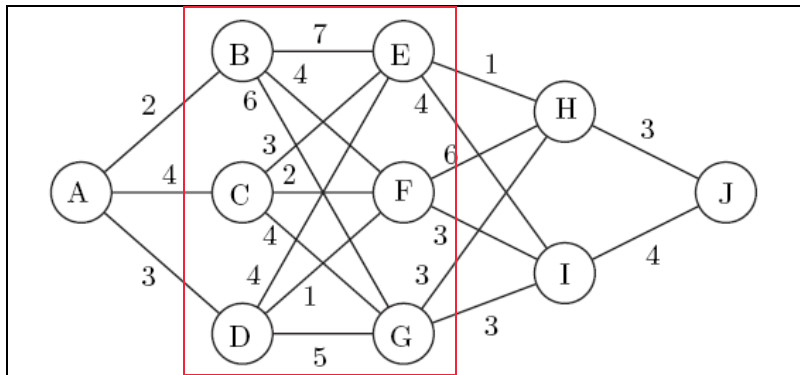


Shortest path construction: 2nd stage (F)

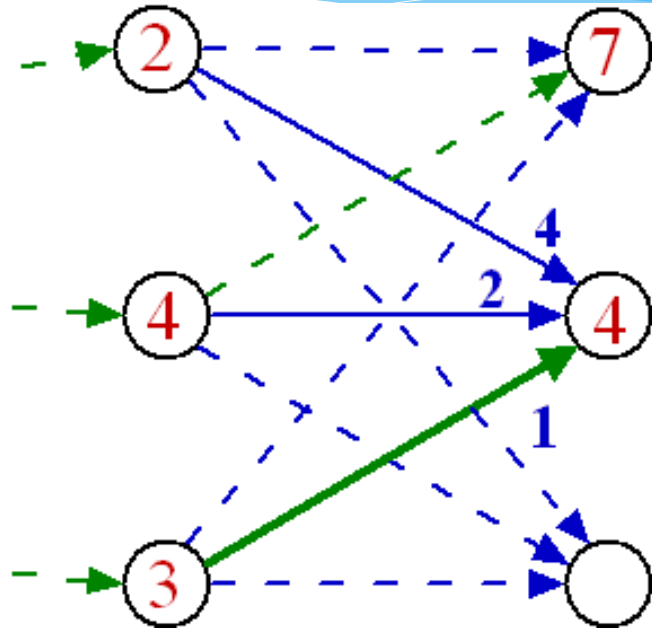


1. (A..B)-F: $2+4=6$
2. (A..C)-F: $4+2=6$
3. (A..D)-F: $3+1=4$ *)

 (A..C)-F: 4

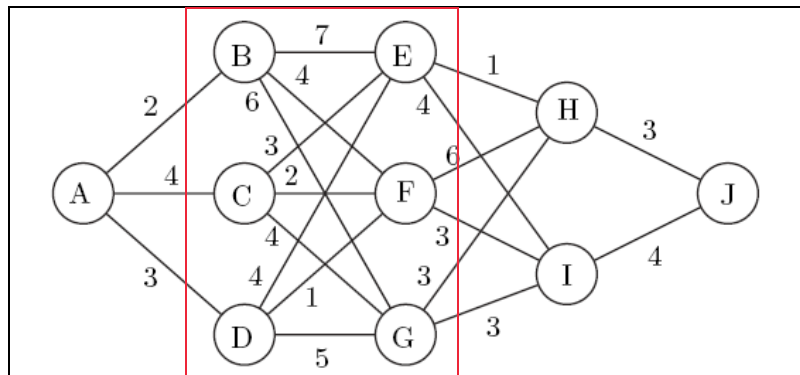


Shortest path construction: 2nd stage (F)

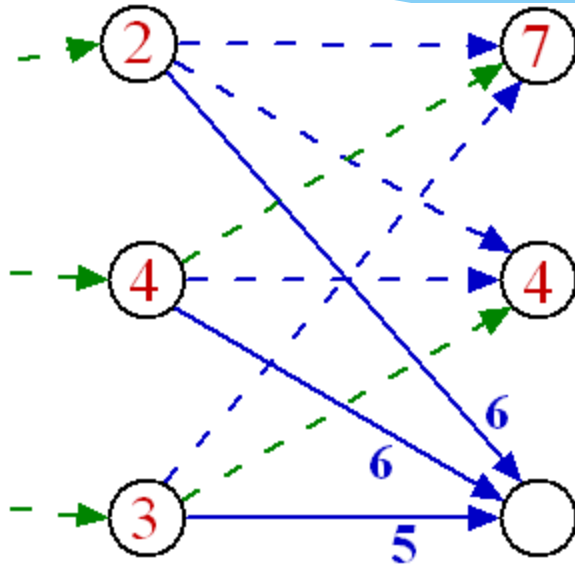


1. (A..B)-F: $2+4=6$
2. (A..C)-F: $4+2=6$
3. (A..D)-F: $3+1=4$ *)

(A..D)-F: 4



Shortest path construction: 2nd stage (G)

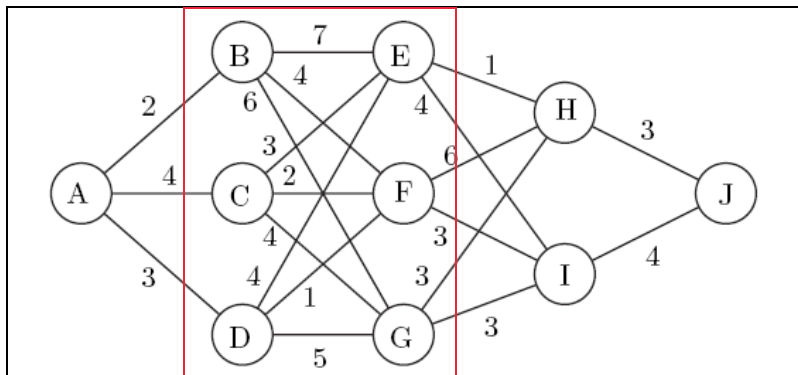


1. (A..B)-G: $2+6=8^*$)

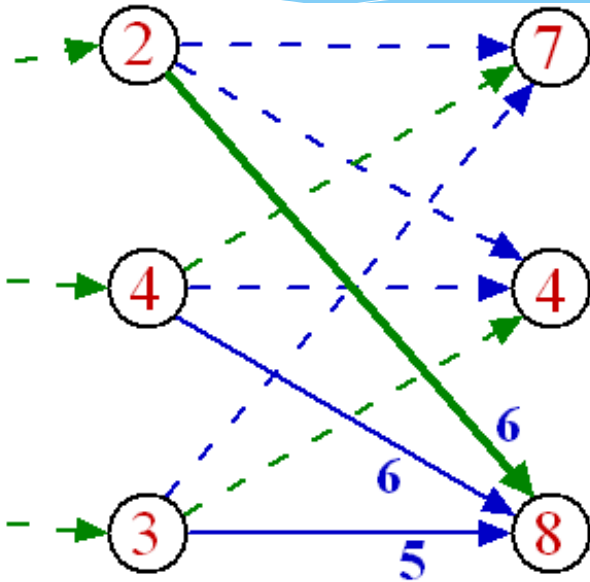
2. (A..C)-G: $4+6=10$

3. (A..D)-G: $3+5=8$

(A..B)-G: 8



Shortest path construction: 2nd stage (G)

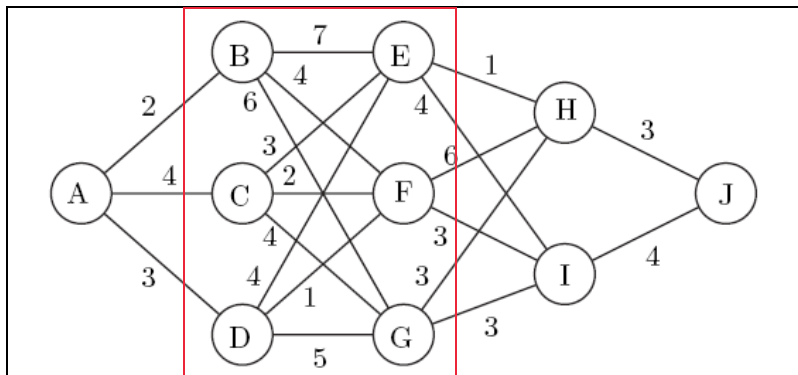


1. (A..B)-G: $2+6=8^*$

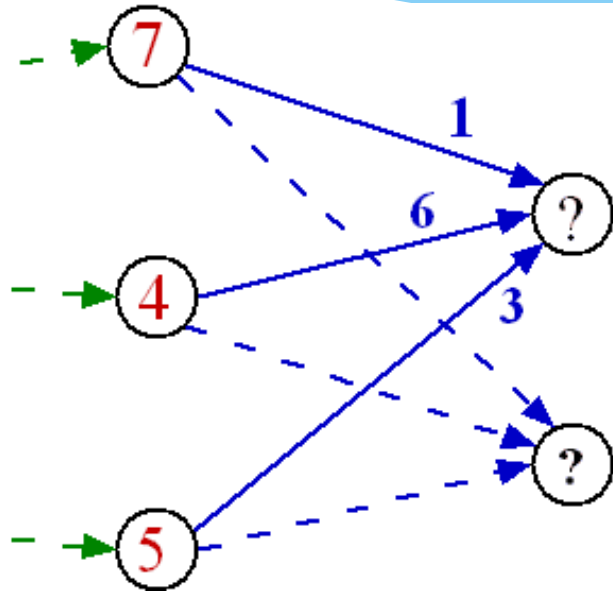
2. (A..C)-G: $4+6=10$

3. (A..D)-G: $3+5=8$

 (A..B)-G: 8



Shortest path construction: 3rd stage (H)

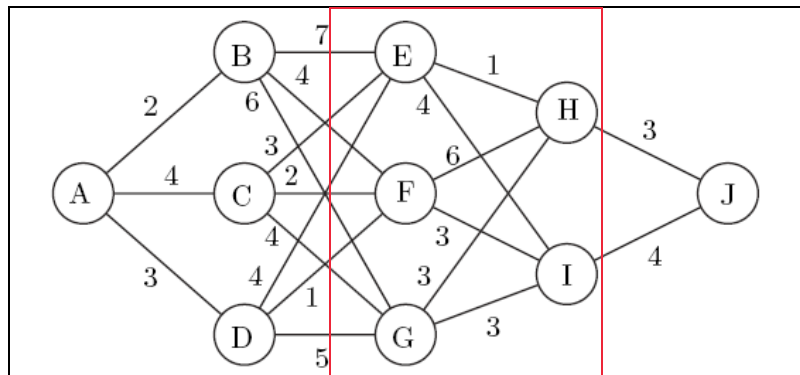


1. (A..E)-H: $7+1=8$ *

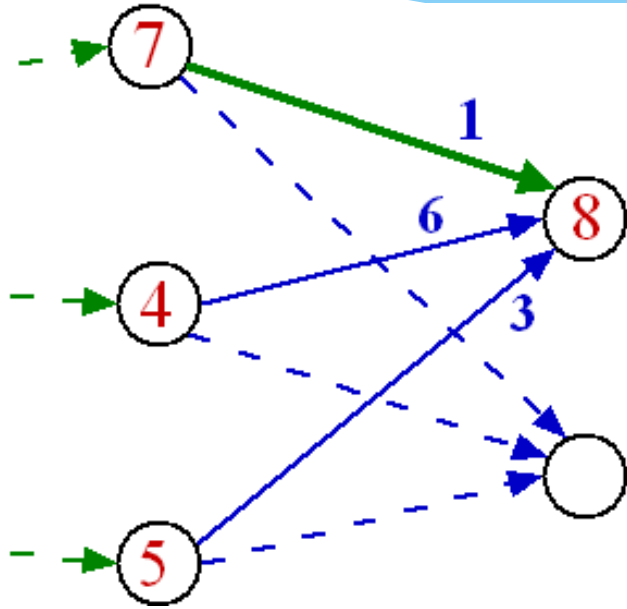
2. (A..F)-H: $4+6=10$

3. (A..G)-H: $5+3=8$

(A..E)-H: 5



Shortest path construction: 3rd stage (H)

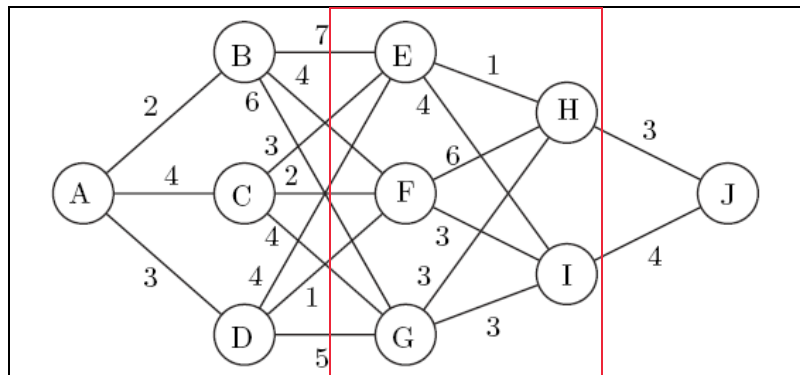


1. (A..E)-H: $7+1=8$ *

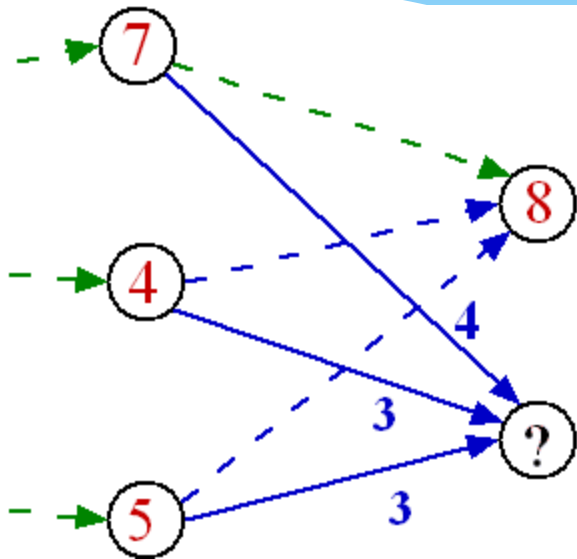
2. (A..F)-H: $4+6=10$

3. (A..G)-H: $5+3=8$

(A..E)-H: 5

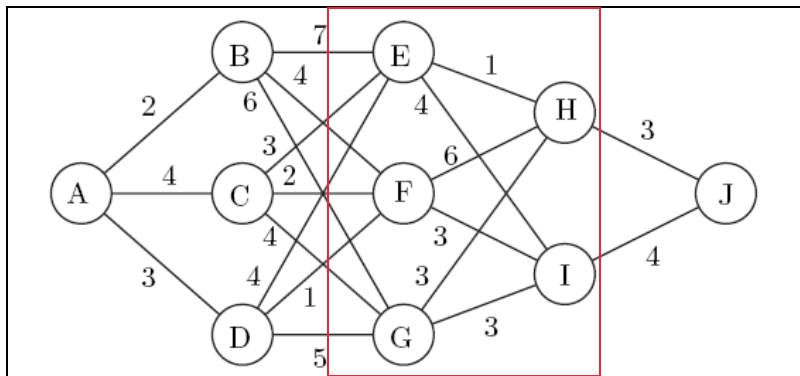


Shortest path construction: 3rd stage (I)

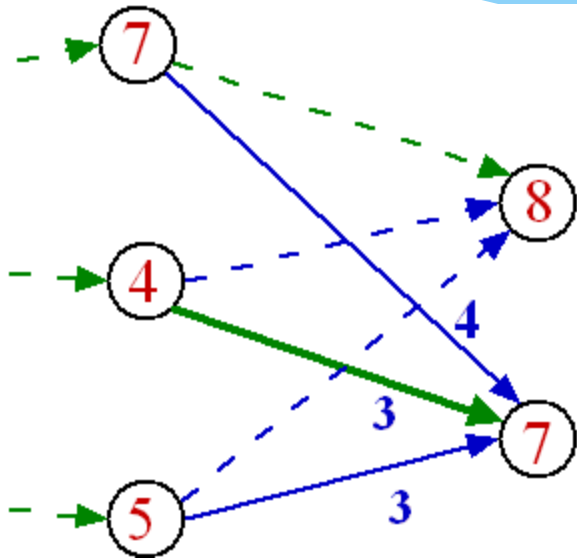


1. (A..E)-I: $7+4=11$
2. (A..F)-I: $4+3=7$ *)
3. (A..G)-I: $5+3=8$

 (A..F)-I: 7

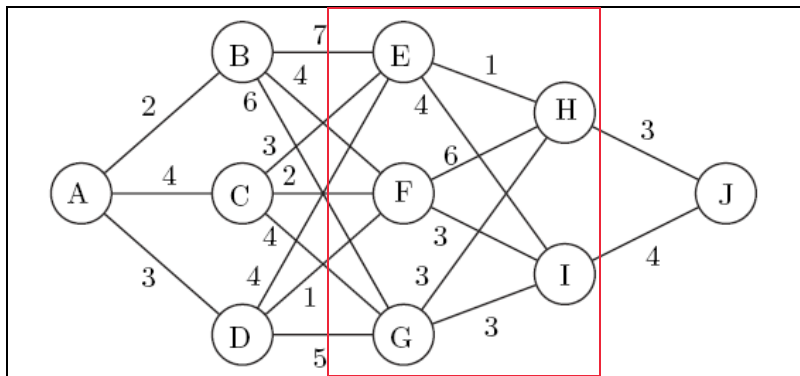


Shortest path construction: 3rd stage (I)

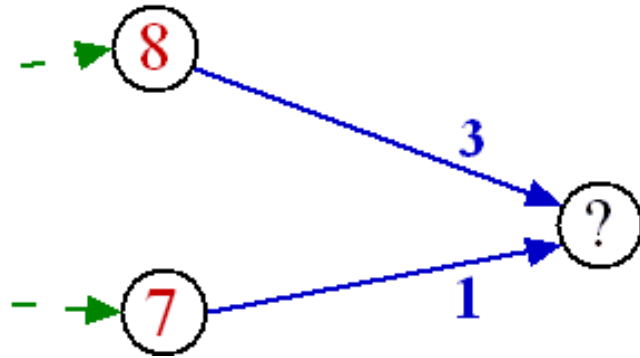


1. (A..E)-I: $7+4=11$
2. (A..F)-I: $4+3=7$ *)
3. (A..G)-I: $5+3=8$

(A..F)-I: 7



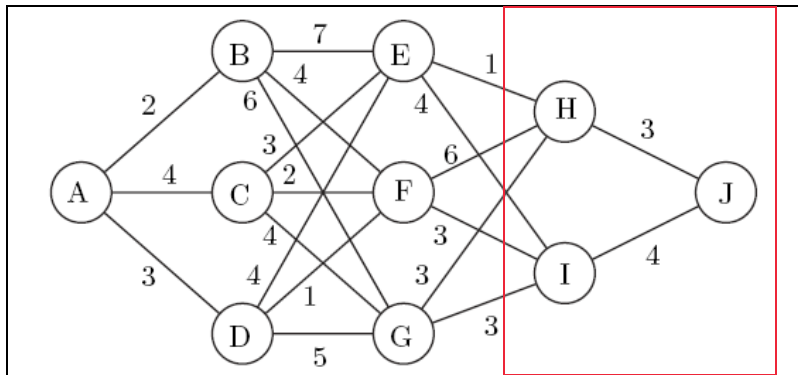
Shortest path construction: 4th stage (J)



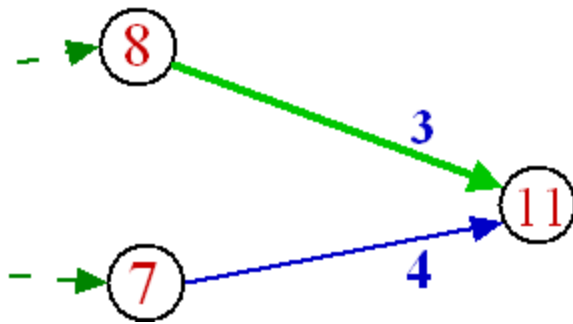
1. (A..H)-J: $8+3=11$ *

2. (A..I) -J: $7+4=11$

(A..H)-J: 11



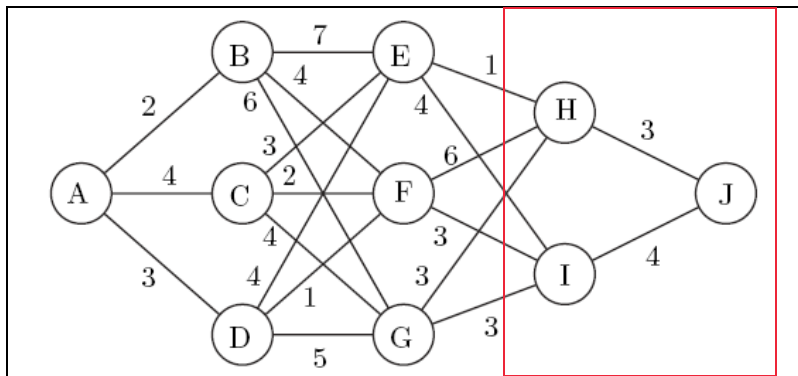
Shortest path construction: 4th stage (J)



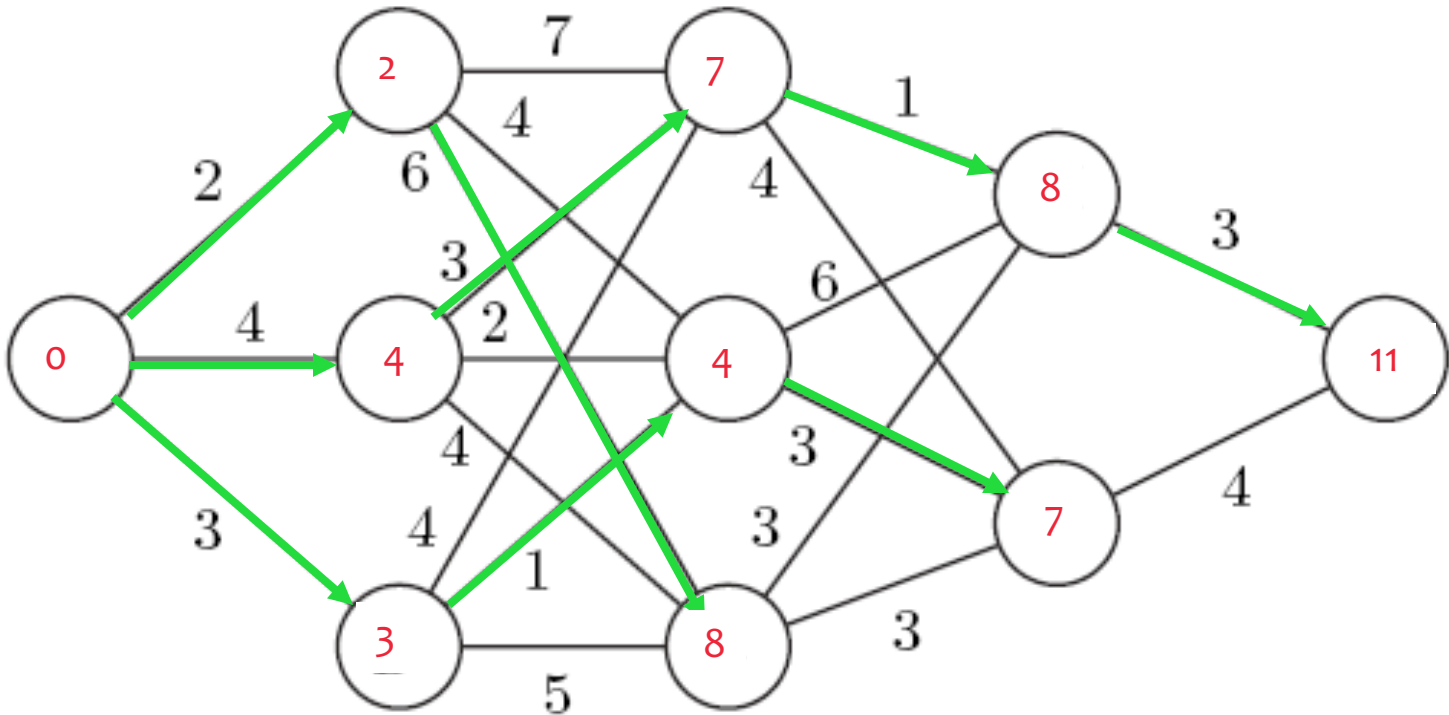
1. (A..H)-J: $8+3=11$ *

2. (A..I) -J: $7+4=11$

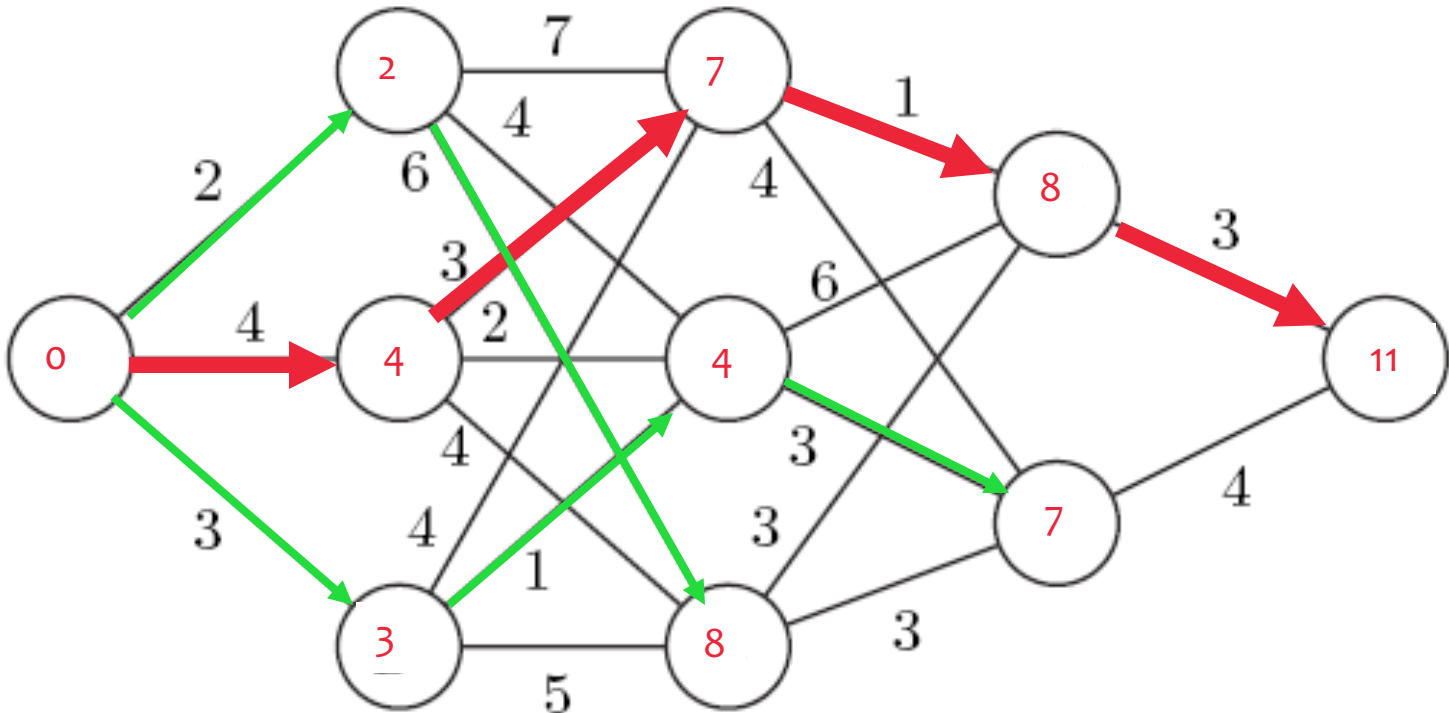
(A..H)-J: 11



Backtrack the shortest path



The shortest path



Route A-C-E-H-J: $4+3+1+3=11$